# INDIAN SCHOOL SOHAR <br> PRE - BOARD EXAMINATION, 2015-16 <br> MATHEMATICS 

Date: 11-02-2016
Time: 3 hrs
Class: $\mathbf{X}$
Max. Marks: 90

## General Instructions:

- All questions are compulsory.
- Section A comprises 4 questions of 1 mark each.
- Section B comprises 6 questions of 2 marks each.
- Section C comprises 10 questions of 3 marks each.
- Section D comprises 11 questions of 4 marks each.


## SECTION A

1. If $p-1, p+3,3 p-1$ are in A.P, then find " $p$ ".
2. If tangents PA and PB from a point P to a circle with centre O are inclined to each other at an angle of $70^{\circ}$, then find $\angle \mathrm{POA}$.
3. If the angle of elevation of a building from a distance of 100 m from its foot is $60^{\circ}$, then find the height of the building.
4.Two cubes each of volume $8 \mathrm{~cm}^{3}$ are joined end to end ,then find the surface area of the resulting cuboid.

## SECTION B

5. What point on the X -axis is equidistant from $(7,6)$ and $(-3,4)$.
6. In a leap year, find the probability that there are 53 Tuesdays in the year.
7. Which term of the A.P., $32,29,26 \ldots \ldots$. is first negative term?
8. Prove that the tangents drawn at the end-points of a diameter of a circle are parallel.
9. Find the value of " $x$ ", if the points $(x, 8),(-4,2)$ and $(5,-1)$ are collinear.
10. Find the middle term(s) of the A.P. $-11,-7,-3$ 49.

## SECTION C

11. Find the roots of the quadratic equation: $a\left(a^{2}+b^{2}\right) x^{2}+b^{2} x-a=0$
12. A card is drawn at random from a well-shuffled pack of 52 playing cards. Find the probability that the card drawn is neither a black card nor a king.
13. The diameter of sphere is 42 cm .It is melted and drawn into a cylindrical wire of 28 cm diameter. Find the length of the wire.
14. Diameter of a wheel is 70 cm .Howmany revolutions will it make to cover 165 meters.
15. Draw a $\triangle \mathrm{ABC}$ with side $\mathrm{BC}=6 \mathrm{~cm}, \mathrm{AB}=5 \mathrm{~cm}$ and $\angle \mathrm{ABC}=60^{\circ}$. Then construct a triangle whose sides are $\frac{3}{4}$ of the corresponding sides of $\triangle \mathrm{ABC}$.
16. An observer 1.5 m tall is 28.5 m away from the chimney. The angle of elevation of the top of the chimney from her eyes is $45^{0}$. Find the height of the chimney.
17. If all the sides of a parallelogram touch a circle, then show that the parallelogram is a rhombus.
18. Find the ratio in which the line $3 x+y=9$ divides the line segment joining the points $(1,3)$ and $(2,7)$
19. Find the sum of the first 31 terms of an AP whose $\mathrm{n}^{\text {th }}$ term is given by $3+\frac{2 n}{3}$
20. Cards marked from 5 to 100 are placed in a box and mixed thoroughly. A card drawn from the box at random. Find the probability that the number on the card taken out is

## (a) a multiple of 5 or 6 (b) a multiple of 5 and 6.

## SECTION D

21. Solve by the method of completing the squares: $5 x^{2}-2 x-2=0$
22. A toy is in the form of a cone mounted on a hemisphere of radius 3.5 cm . If the total height of the toy is 15.5 cm ,find its total surface area.
23. The minute hand of a clock is 10 cm long. Find the area on the face of the clock described by the minute hand between 9 am and 9.35 am .
24. If $P(2,1), Q(3,2)$ and $R(4,6)$ are the mid points of sides of $A B, B C$ and $C A$ respectively in the triangle ABC , find the coordinates of points $\mathrm{A}, \mathrm{B}$ and C .
25. The angle of elevation of a jet plane from a point $P$ on the ground is $60^{\circ}$.After a flight of 15 seconds, the angle of elevation changes to $30^{\circ}$.If the jet plane is flying at a constant height of $1500 \sqrt{3} \mathrm{~m}$, find the speed of the jet plane.
26. Draw a pair of tangents to a circle of radius 5.5 cm , which are inclined to each other at an angle of $60^{\circ}$.
27. From a point $P$, two tangents $P A$ and $P B$ are drawn to a circle $C(O, r)$.If $O P=2 r$, Show that $\Delta A P B$ is equilateral.
28. The rate at which the monthly salary of a person increases annually is an A P. If he was drawing Rs 4500 p.m.in his $11^{\text {th }}$ year of service and Rs 6900 p.m. in his $27^{\text {th }}$ Year of service, find his salary at the start and the annual increment.
29. Two years ago a man's age was three times the square of his son's age. Three years hence his age will be four times his son's age. Find their present ages.
30. A metallic right circular cone 20 cm high and whose semi-vertical angle is $30^{\circ}$, is cut into two parts at the middle of its height by a plane parallel to its base. If the frustum so obtained be drawn into a wire of diameter $\frac{1}{3} \mathrm{~cm}$, find the length of the wire.
31. In an equilateral triangle of side 24 cm , a circle is inscribed touching its side. Find the area of the remaining portion of the triangle. $(\sqrt{3}=1.732)$
