# INDIAN SCHOOL SOHAR FINAL EXAM – 2015-16 MATHEMATICS

MARKS: 100 TIME: 3Hrs

## **GENERAL INSTRUCTIONS**

- 1. All questions are compulsory.
- 2. The question paper consists of 26 questions divided into three sections A, B and C. Section A comprises of 6 questions of one mark each, section B comprises of 13 questions of four marks each and section C comprises of 7 questions of six marks each.
- 3. All questions in Section A are to be answered in one word, one sentence or as per the exact requirement of the question.
- 4. There is no overall choice. However, an internal choice has been provided in 4 questions of four marks each and 2 questions of six mark each. You have to attempt only one of the alternatives in all such questions.
- 5. Use of calculators is not permitted.

# **SECTION - A**

- 1. Find the ratio in which the line segment joining the points (4, 8, 10) and (6, 10, -8) is divided by the YZ-plane.
- 2. Name the octants in which the following points lie:

(1,-2, 3), (-4, -2, 3), (4, -2, -5), (4, 2, -5)

- 3. Write the contrapositive of the following statement: *"If a triangle is equilateral, it is isosceles".*
- 4. For the following statements, determine whether an inclusive "Or" or exclusive "Or" is used. Give reasons for your answer.

"The school is closed if it is a holiday or a Sunday".

- 5. If 4x + i(3x y) = 3 + i(-6), where x and y are real numbers, then find the values of x and y.
- 6. The minute hand of a watch is 1.5 cm long. How far does its tip move in 40 minutes? (Use  $\pi = 3.14$ ).

## **SECTION – B**

- 7. Prove that for any real numbers x and y,  $\cos x = \cos y$ , implies  $x = 2n\pi \pm y$ , where  $n \in \mathbb{Z}$
- 8. In any  $\triangle ABC$ , prove that :  $sin\left(\frac{B-C}{2}\right) = \frac{b-c}{a}\cos\frac{A}{2}$

- 9. Prove the following by using the principle of mathematical induction for all  $n \in N$ :  $\left(1 + \frac{3}{1}\right)\left(1 + \frac{5}{4}\right)\left(1 + \frac{7}{9}\right) \dots \dots \left(1 + \frac{(2n+1)}{n^2}\right) = (n+1)^2$
- 10. Let A, B, and C be the sets such that  $A \cup B = A \cup C$  and  $A \cap B = A \cap C$ . Show that B = C.
- 11. Find the domain and the range of the real function f defined by  $f(x) = \sqrt{16 x^2}$

12. Show that : 
$$\frac{1 \times 2^2 + 2 \times 3^2 + \dots + n \times (n+1)^2}{1^2 \times 2 + 2^2 \times 3 + \dots + n^2 \times (n+1)} = \frac{3n+5}{3n+1}$$

The difference between any two consecutive interior angle of a polygon is  $5^0$ . If the smallest angle is  $120^0$ , find the number of the sides of the polygon.

13. If *p*, *q*, *r* are in G.P. and the equations,  $px^2 + 2qx + r = 0$  and  $dx^2 + 2ex + f = 0$  have a common root, then show that  $\frac{d}{p}$ ,  $\frac{e}{q}$ ,  $\frac{f}{r}$  are in A.P.

14. If Z = x + iy, prove that  $|x| + |y| \le \sqrt{2}|Z|$ OR

Convert the complex number  $z = \frac{-16}{1+i\sqrt{3}}$  into the polar form.

15. Find the derivative of  $f(x) = x \sin x$  from the first principle with respect to x.

Evaluate: 
$$\lim_{x \to 0} \frac{1 - \cos x \sqrt{\cos 2x}}{x^2}$$

- 16. Find the equation of the line through the point (4, 5) and make equal angles with the lines 5x 12y + 6 = 0 and 3x = 4y + 7.
- 17. If 4-digit numbers greater than 5000 are randomly formed from the digits 0,1,3,5 and 7, what is the probability of forming a number divisible by 5 when, the repetition of digits is not allowed?

#### OR

Twelve balls are distributed among three boxes, find the probability that the first box will contain three balls.

- 18. The letters of the word 'MOTHER' are written in all possible orders and these words are written out as in a dictionary. Find the rank of the word 'MOTHER'.
- 19. How many words can be formed by taking 4 letters at a time out of the letters of the word "MATHEMATICS".

#### <u>SECTION – C</u>

- 20. In a town of 10,000 families it was found that 40% families buy newspaper A, 20% families buy newspaper B and 10% families buy newspaper C. 5% families buy A and B, 3% families buy B and C and 4% families buy A and C. If 2% families buy all the three newspapers, find the number of families which buy i) A only ii) B only iii) none of A, B and C. Mention any 2 importance of reading newspaper every day.
- 21. Solve the following system of inequalities graphically:

$$x \ge 0, y \ge 0, 3x + 2y \le 150, x + 4y \le 80, x \le 20$$

22. Find n, if the ratio of the fifth term from the beginning to the fifth term from the end in

the expansion 
$$\left(\sqrt[4]{2} + \frac{1}{\sqrt[4]{3}}\right)^n$$
 is  $\sqrt{6}$  : 1  
OR

The  $3^{rd}$ ,  $4^{th}$  and  $5^{th}$  terms in the expansion of  $(x+a)^n$  are respectively 84,280 and 560. Find the values of x, a and n.

- 23. Find the coordinate of the foci, the vertices, the length of major axis, the minor axis, the eccentricity and the length of latus rectum of the conic:  $3 x^2 + 2y^2 = 18$ .
- 24. Find the points on the line x + y = 4 which lie at a unit distance from the line 4x+3y = 10.
- 25. Prove that  $:2\cos\frac{\pi}{13}\cos\frac{9\pi}{13} + \cos\frac{3\pi}{13} + \cos\frac{5\pi}{13} = 0$ OR

Prove that:  $sin^2 x + sin^2 \left(x + \frac{\pi}{3}\right) + sin^2 \left(x - \frac{\pi}{3}\right) = \frac{3}{2}$ 

26. Calculate mean and standard deviation for the following distribution.

Classes	30-40	40 - 50	50-60	60 - 70	70-80	80 - 90	90 - 100
Frequency	3	7	12	15	8	3	2

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