

INDIAN SCHOOL SOHAR PERIODIC TEST II (2019-20) SUBJECT: MATHEMATICS

CLASS: X DATE: 19.09.2019

General Instructions:

- > The question paper consists of 40 questions divided into four sections A, B, C and D.
- Section A contains 20 questions of 1 mark each, Section B contains 6 questions of 2 marks each
- Section C contains 8 questions of 3 marks each and Section D contains 6 questions of 4 marks each.
- > Use of calculator is not permitted.

SECTIONA

(d) 5 + $\sqrt{25}$

1. Which of the following is not an irrational number?

(a) 5 - $\sqrt{3}$ (b) $\sqrt{5} + \sqrt{3}$ (c) 7 + $\sqrt{2}$

- 2. The height and length of the shadow of a man are the same, then find the angle of elevation of the sun.
 - (a) 30° (b) 45° (c) 60° (d) 90°
- 3. The graph of the polynomial p(x) intersects the X- axis four times in distinct points, then Which of the following could be an expression for p(x)?

(a)
$$3x + 3$$
 (b) $x^3 + 3x^2 - 0x^4 + 3$ (c) $x^4 - 3$ (d) $x^2 - 9$.

4. In the equations Ax + By + C = 0 and Px + Qy + R = 0, if
$$\frac{A}{P} \neq \frac{B}{Q}$$
, then which type of lines will

these equations represent.

(a) Parallel lines (b) Intersecting lines (c) coinciding lines (d) Terminated lines.

5. Find the solution of 3x - y = 8 and x + y = 4.

(a) x = 3, y = -1 (b) x = 3, y = 1 (c) x = -3, y = 1 (d) x = -3, y = -1

- 6. Find the value of cos38° cos52° sin38° sin52°
 - (a) -1 (b) 1 (c) 0 (d) Not Defined.

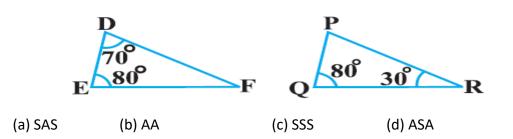
7. In $\triangle ABC$, $\angle C = 90^{\circ}$, then find the value of sin²A + sin²B

- (a) 0 (b)-1 (c) 1 (d) Not Defined
- 8. Which of the following cannot be the sides of a right triangle?

(a) 9cm,15cm,12cm (b) 2cm,1cm, $\sqrt{5}$ cm (c) 6cm,8cm,10cm (d) 9cm 5cm,7cm

- 9. 10. If D > 0 in a quadratic equation, then the nature of its roots will be
 - (a) equal roots (b) unequal real roots (c) no real roots (d) imaginary roots.

10. Which of the following similarity criterion used to prove $\Delta DEF \sim \Delta PQR$.



11. After how many places of decimal the decimal expansion of the rational number $\frac{47}{2^2.5}$ will

terminate.

- 12. If $x = 2^3 \times 3 \times 5^2$, $y = 2^2 \times 5^2$, then find HCF (x,y).
- 13. If α , β are the zeroes of the polynomial $x^2 5x + 8$, then find the value of $\alpha + \beta$.

OR

If A, B are the zeroes of the polynomial $ax^2 + bx + c$, then find the value of AB.

- 14. If both the zeros of a quadratic polynomial ax² + bx + c are equal and opposite in sign, then find" b "
- 15. Find the number of solutions of the pair of linear equations x + 2y = 8 and 2x + 4y = 16.
- 16. If the lines given by 3x + 2ky = 2 and 2x + 5y = -1 are parallel, then find the value of "k".
- 17. Find the value of (tan 1^0 tan 3^0 tan 87^0 tan 89^0)

OR

If
$$\cos 3\theta = \frac{\sqrt{3}}{2}$$
, then find the value of θ .

- 18. If $\sin \alpha = \frac{1}{2}$ and $\cos \beta = \frac{1}{2}$, then find the value of $\alpha + \beta$
- 19. If 2 is a root of the equation $x^2 + kx 5 = 0$, then find the value of "k".
- 20. A girl said, "the product of my age 5 years before and after 5 years is 75". What is her present age?

SECTIONB

- 21. Show that 8ⁿ cannot end with the digit zero for any natural number n.
- 22. The areas of two similar triangles ABC and PQR are 25 cm² and 49 cm² respectively.

If QR = 9.8 cm, then find BC.

23. Find the nature of roots of the quadratic equation $4x^2 + 4\sqrt{3}x + 3 = 0$.

24. If the diagonals of a quadrilateral divide each other proportionally, prove that it is a trapezium.

OR

S and T are points on sides PR and QR of $\triangle PQR$ such that $\angle P = \angle RTS$. Show that $\triangle RPQ \sim \triangle RTS$. 25. If $\sqrt{3} \tan \theta = 1$, find the value of $\sin^2 \theta - \cos^2 \theta$

OR

Evaluate: sin 60° cos 30° + sin 30° cos 60°

26. Solve for "a" and "b":
$$\sqrt{2}$$
 a + $\sqrt{3}$ b = 0 , $\sqrt{3}$ a - $\sqrt{8}$ b = 0.

SECTION C

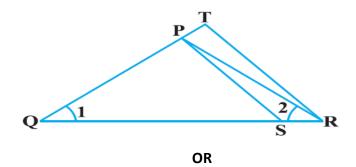
27. Solve for x: $\frac{4}{x} - 3 = \frac{5}{2x+3}$.

OR

Solve by the method of completing the squares: $x^2 - 3x - 10 = 0$.

28. The shadow of a tower standing on a level ground is found to be 40 m longer when the Sun's altitude is 30° than when it is 60°. Find the height of the tower.

29. In Fig.
$$\frac{QR}{QS} = \frac{QT}{PR}$$
 and $\angle 1 = \angle 2$. Show that \triangle PQS $\sim \triangle$ TQR.



Prove that the sum of the squares of the sides of a rhombus is equal to the sum of the squares of its diagonals.

30. The age of a father is equal to sum of the ages of his 6 children. After 15 years, twice the age of the father will be the sum of ages of his children. Find the age of the father.

OR

Solve for "x" and "y": px + qy = p - q and qx - py = p + q

31. Prove that $\sqrt{7}$ is irrational.

- 32. Find the zeros of a quadratic polynomial $6x^2 3 7x$ and verify the relationship between the zeros and the coefficients .
- 33. If a and b are two odd positive integers such that a > b, then prove that one of the two numbers $\frac{a+b}{2}$ and $\frac{a-b}{2}$ is odd and the other is even.
- 34. Find all the zeros of the cubic polynomial $x^3 x^2 3x + 3$, one of its zero is "1".

SECTION D

35. A railway half ticket costs half the full fare, but the reservation charges are same on a half or full ticket. One reserved a full ticket at Rs 2530. Also one reserved a full ticket and a half ticket at Rs 3810. Find the full ticket charge and reservation charge for a ticket.

36. Prove the following trigonometric identities: (1) $\sin^2 A + \cos^2 A = 1$ (2) $\sec^2 A - \tan^2 A = 1$

37. Prove that, $\frac{\tan\theta + \sec\theta - 1}{\tan\theta - \sec\theta + 1} = \frac{1 + \sin\theta}{\cos\theta}$

OR

Prove that,
$$\frac{\cot\theta + \csc\theta - 1}{\cot\theta - \csc\theta + 1} = \frac{1 + \cos\theta}{\sin\theta}$$

- 38. From a point 100m above a lake, the angle of elevation of a helicopter is 30^o and the angle of depression of reflection of the helicopter in the lake is 60^o. Find the height of the helicopter.
- 39. If a line is drawn parallel to one side of a triangle to intersect the other two sides in distinct points, prove that the other two sides are divided in the same ratio.

OR

Prove that, in a right triangle the square of the hypotenuse is equal to the sum of the squares of the other two sides.

40. The speed of a boat in still water is 15km/hr. it can go 30km upstream and return downstream to the original point in 9/2 hours .Find the speed of the stream
