## INDIAN SCHOOL SOHAR <br> PRE-BOARD EXAMINATION (2019-20) <br> MATHEMATICS-STANDARD

CLASS: X
DATE: 25/01 /2020

MAX. MARKS: $\mathbf{8 0}$
DURATION: 3 HRS

## General Instructions:

1. All questions are compulsory
2. The question paper consists of 40 questions divided into 4 sections $A, B, C$ and $D$.
3. Section A comprises of 20 questions of 1 mark each. Section B comprises of 6 questions of 2 marks each. Section C comprises of 8 questions of 3 marks each. Section D comprises of 6 questions of 4 marks each.
4. There is no overall choice. However, an internal choice has been provided in two questions of 1 mark each, two questions of 2 marks each, three questions of 3 marks each and three questions of four marks each.You have to attempt only one of the alternatives in all such questions.
5. Use of calculators is not permitted.

## SECTION A

## (Q.1-Q.10) are multiple choice questions. Select the appropriate answer from the given options.

1. If $\operatorname{HCF}(a, 8)=4, \operatorname{LCM}(a, 8)=24$, then $a$ is:
(a) 8
(b) 10
(c) 12
(d) 14
2. The mode is equal to
a) 2 Median -3 Mean
(b) 3 Median + 2 Mean
(c) 3 Median - 2 Mean
(d) 2 Median +3 Mean
3. H.C.F. of two co-prime numbers is :
(a) 1
(b) 2
(c) 0
(d) 3
4. The graphical representation of the pair of equations $x+2 y-4=0$ and $2 x+4 y-12=0$ is :
(a) Intersecting lines
(b) Parallel lines
(c) Coincident lines
(d) All the above
5. If $\sin \theta=\cos \theta$, the value of $\operatorname{cosec} \theta$ is
(a) 2
(b) 1
(c) $\frac{2}{\sqrt{3}}$
(d) $\sqrt{2}$
6. If $\sqrt{2} \sin \left(60^{\circ}-\alpha\right)=1$, then $\alpha$ is
(a) $45^{\circ}$
(b) $15^{\circ}$
(c) $60^{\circ}$
(d) $30^{\circ}$
7. Which of the following is not defined ?
(a) $\cos 0^{\circ}$
(b) $\tan 45^{\circ}$
(c) $\sec 90^{\circ}$
(d) $\sin 90^{\circ}$
8. $A O B C$ is a rectangle whose three vertices are $A(0,3), O(0,0)$ and $B(5,0)$. The length of its diagonal is
(a) 5
(b) 3
(c) $\sqrt{34}$
(d) 4
9. The area of a triangle with vertices $A(3,0), B(7,0)$ and $C(8,4)$ is
(a) 8
(b) 28
(c) 14
(d) 6
10. If the distance between the points $(p, 4)$ and $(0,1)$ is 5 , then the value of $p$ is
(a) 4 only
(b) 0
(c) -4 only
(d) $\pm 4$

## (Q.11-Q.15) Fill in the blanks

11. The radii of two cylinder are in the ratio $2: 3$ and their heights are in the ratio $5: 3$. The ratio of their volume is $\qquad$
12. The value(s) of $k$ such that the equation $k x^{2}+6 x+k=0$ has equal roots is (are) $\qquad$
OR
The graph of $y=p(x)$ given below. The number of zeroes of $p(x)$ is $\qquad$

13. $P Q$ is drawn parallel to the base $B C$ of a $\triangle A B C$ cutting $A B$ at $P$ and $A C$ at $Q$. If $A B=4 B P$ and $C Q=2 \mathrm{~cm}$, then $A C$ is equal to $\qquad$ cm
14. If the common difference of an A.P. is 5, then the value of $a_{18}-a_{14}$ is $\qquad$
15. A girl calculates the probability of her winning the game in a match is 0.08 . The probability of her losing the game is $\qquad$

## (Q.16-Q.20) Answer the following

16. After how many places will the decimal expansion of $\frac{14587}{1250}$ terminate?
17. If the ratio of the corresponding sides of two similar triangles is $3: 4$, then what is the ratio of their perimeters?
18. If $O$ is centre of a circle, $P Q$ is a chord and the tangent $P R$ at $P$ makes an angle of $50^{\circ}$ with $P Q$, then what is measure of $\angle \mathrm{POQ}$ ?


## OR

From a point $Q$, the length of the tangent to a circle is 24 cm and the distance of $Q$ from the centre is 25 cm . Find the radius of the circle.
19. What is the $10^{\text {th }}$ term of the sequence $\sqrt{2}, \sqrt{8}, \sqrt{18}, \ldots \ldots$
20. If $\frac{1}{2}$ is a root of the equation $x^{2}+k x-\frac{5}{4}=0$, then what is the value of $k$ ?

## SECTION B

21. Which term of the A.P. $-2,-7,-12$.....will be -77 ?
22. If all the sides of a parallelogram touch a circle, show that the parallelogram is a rhombus
23. In the given figure, If $L D \perp M N$, then Prove that $L M^{2}+D N^{2}=L N^{2}+M D^{2}$


## OR

Tina is fly fishing in a stream. The tip of her fishing rod is 1.8 m above the surface of the water and the fly at the end of the rests on the water 3.6 m away and 2.4 m from a point directly under the tip of the rod. Assuming that the string ( from the tip of the rod to the fly) is taut, how much string should she have out?

24. Prove that $(\sqrt{3}+1)\left(3-\cot 30^{\circ}\right)=\tan ^{3} 60^{\circ}-2 \sin 60^{\circ}$
25. A lot consists of 48 mobile phones of which 42 are good, 3 have only minor defects and 3 have major defects. Tanya will buy a phone if it is good but the trader will only buy a phone if it has no major defect. A phone is selected at random from the lot. What is the probability that it is
i) Acceptable to Tanya
ii) Acceptable to the trader

## OR

Two dice are thrown at the same time and the product of the numbers appearing on it is noted. Find the probability that the product is less than 9
26. A wooden article was made by scooping out a hemisphere from each end of a solid cylinder as shown in the figure .If the height of cylinder is 10 cm and its base radius is 3.5 cm . Find the total surface area of article. $\left(U s e \pi=\frac{22}{7}\right)$

## SECTION C

27. Use Euclid's algorithm to find the HCF of 441,567 and 693.

OR
Prove that $\sqrt{2}$ is an irrational number
28. If sum of first 6 terms of an A.P. is 36 and that of the first 16 terms is 256 , find the sum of the first 10 terms.
29. Solve $\frac{4}{x}+3 y=14, \quad \frac{3}{x}-4 y=23$

## OR

A takes 3 hours more than $B$ to walk 30 km but if $A$ doubles his pace, he is ahead of $B$ by $1 \frac{1}{2}$ hours. Find their speeds of walking.
30. Divide $p(x)=x^{4}-5 x+6$ by $g(x)=2-x^{2}$ and find the quotient and the remainder.
31. In a rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each. 100 flower pots have been placed at a distance of 1 m from each along AD. Niharika runs $\frac{1}{4}$ th the distance AD on the second line and posts a green flag and Priya runs $\frac{1}{5}$ th the distance AD on the eighth line and posts a red flag. What is the distance between the two flags ? If Rashmi posts a blue flag exactly halfway between the line segment joining the flags, where should she post her flag?

32. If $1+\sin ^{2} \theta=3 \sin \theta \cos \theta$, then prove that $\tan \theta=1$ or $\frac{1}{2}$

OR
Evaluate $\frac{\cos ^{2} 20^{\circ}+\cos ^{2} 70^{\circ}}{\sec ^{2} 50^{\circ}-\cot ^{2} 40^{\circ}}+2 \operatorname{cosec}^{2} 58^{\circ}-2 \cot 58^{\circ} \tan 32^{\circ}$
33. In the given figure, a semicircle is drawn on $A B$ as diameter, and $O$ is center. Semi circular flower beds are formed on $A O$ and $O B$ as diameters. If $A B$ is 28 m , find the area of the shaded region.

34. Change the following frequency distribution to less than type distribution and draw its ogive

| Classes | $0-5$ | $5-10$ | $10-15$ | $15-20$ | $20-25$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency f | 6 | 8 | 10 | 6 | 4 |

## SECTION D

35. Draw a right triangle $\triangle \mathrm{ABC}$ in which $\mathrm{BC}=12 \mathrm{~cm}, \mathrm{AB}=5 \mathrm{~cm}$ and $\angle B=90^{\circ}$. Construct a triangle similar to it and of scale factor $\frac{2}{3}$. Is the new triangle also a right triangle ?

OR
Draw a circle of radius 3 cm . Construct a pair of tangents to it, which are inclined to each other at an angle of $45^{\circ}$.
36. Prove that in a right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.
37. A fast train takes 3 hour less than a slow train for a journey of 600 km . If the speed of the slow train is $10 \mathrm{~km} / \mathrm{hr}$ less than that of the fast train, find the speeds of the two trains.

OR
Solve : $\frac{1}{(2 x-3)}+\frac{1}{(x-5)}=1, \mathrm{x} \neq 5, \frac{3}{2}$
38. Find the volume of the largest solid right circular cone that can be cut out of a solid cube of side 14 cm . Also find the slant height of the cone. $\left(U \operatorname{se} \pi=\frac{22}{7}\right)$

## OR

A cylindrical vessel with internal diameter 10 cm and height 10.5 cm is full of water. A solid cone of base diameter 7 cm height 6 cm is completely immersed in water. Find the volume of (i) Water displaced out of the cylindrical vessel
(ii) Water left in the cylindrical vessel. (Use $\pi=\frac{22}{7}$ )
39. The angles of depression of the top and bottom of an 8 m tall building from the top of a multi-storeyed building are $30^{\circ}$ and $45^{\circ}$ respectively. Find the height of the multi-storeyed building and the distance between the two buildings.
40. Find the mean, mode and median of the following distribution.

| Classes | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $f$ | 6 | 5 | 12 | 22 | 15 |

